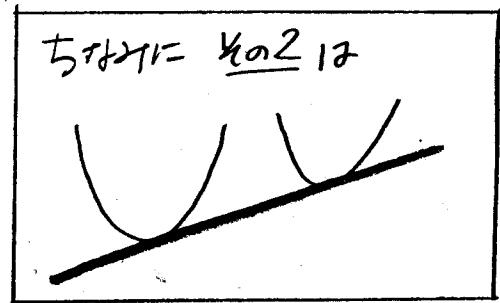
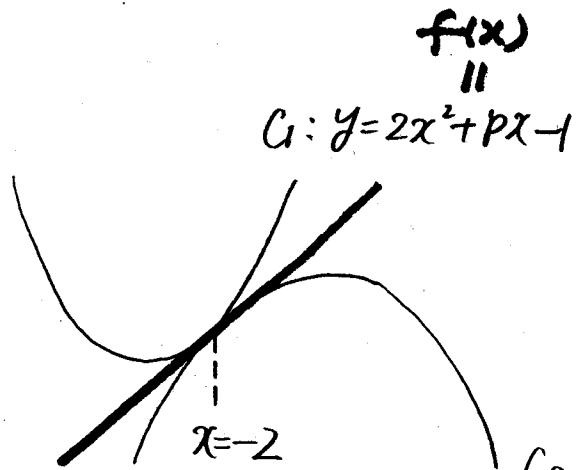


[80]



共通接線 x の 1

〈ポイント〉 ① $x = -2$ のときの y の値が一致。

② $x = -2$ での接線の傾きが一致。

① $f(-2) = g(-2)$ だから

$$-8 - 2p - 1 = -4 - 4 + 9$$

$$-2p + 9 = 15$$

② $f'(x) = 4x + p$, $g'(x) = -2x + 2$

$f'(-2) = g'(-2)$ だから

$$-8 + p = 4 + 2$$

$$p = 14$$

①, ② より $\underline{p = 14, q = -13}$

$$[85] \quad y = x^3 - 4x^2 + 4x \quad (= x(x-2)^2)$$

$$y' = 3x^2 - 8x + 4$$

$$= (x-2)(3x-2)$$

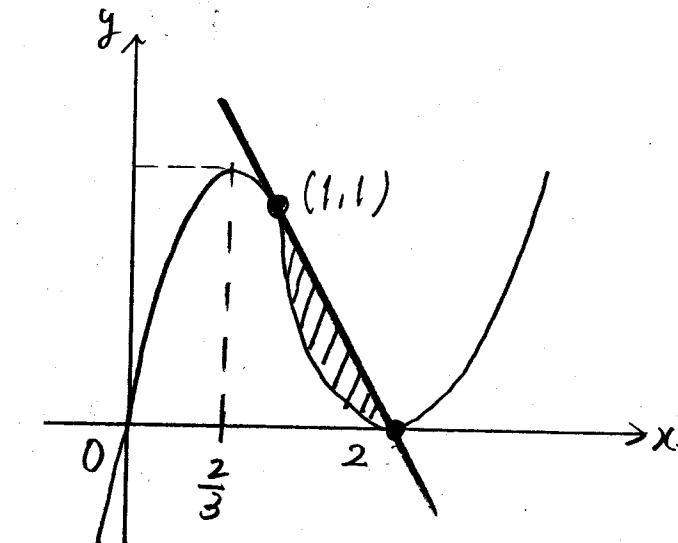
x	...	$\frac{2}{3}$...	2	...
y'	+	0	-	0	+
y	↗ 極大		↘ 極小		↗

接点 $(1, 1)$

$$y' = 3x^2 - 8x + 4$$

$$\downarrow \quad x = 1 \text{ を代入}$$

（負号） -1



接線は $y - 1 = -(x - 1)$

$$y = -x + 2$$

$(2, 0)$ を通る!!

$$S = \int_1^2 \{-x+2 - (x^3 - 4x^2 + 4x)\} dx$$

$$= \int_1^2 (-x^3 + 4x^2 - 5x + 2) dx$$

$$= -\frac{1}{4}[x^4]_1 + \frac{4}{3}[x^3]_1 - \frac{5}{2}[x^2]_1 + 2[x]_1$$

$$= -\frac{1}{4}(16-1) + \frac{4}{3}(8-1) - \frac{5}{2}(4-1) + 2(2-1)$$

$$= -\frac{15}{4} + \frac{28}{3} - \frac{15}{2} + 2$$

$$= \frac{-45 + 112 - 90 + 24}{12} = \frac{1}{12}$$

[86] $C: y = x^2$ ↪ 次のまき m , $(1, 2)$ を通る
 $\ell: y = m(x-1) + 2$

(1) $x^2 = m(x-1) + 2$

$x^2 - mx + m - 2 = 0$

$$x = \frac{m \pm \sqrt{m^2 - 4m + 8}}{2}$$

(2)

$$S = \frac{1}{6} \left(\frac{m+\sqrt{8}}{2} - \frac{m-\sqrt{8}}{2} \right)^3$$

$$= \frac{1}{6} (\sqrt{m^2 - 4m + 8})^3$$

(3)

$$S = \frac{1}{6} (\sqrt{(m-2)^2 + 4})^3$$

$m=2$, $\sigma \in \mathbb{R}$

$$\text{Min } \frac{1}{6} (\sqrt{4})^3 = \frac{1}{6} \times 2^3 = \frac{4}{3},$$